

# Shelving spectroscopy of the strontium intercombination line

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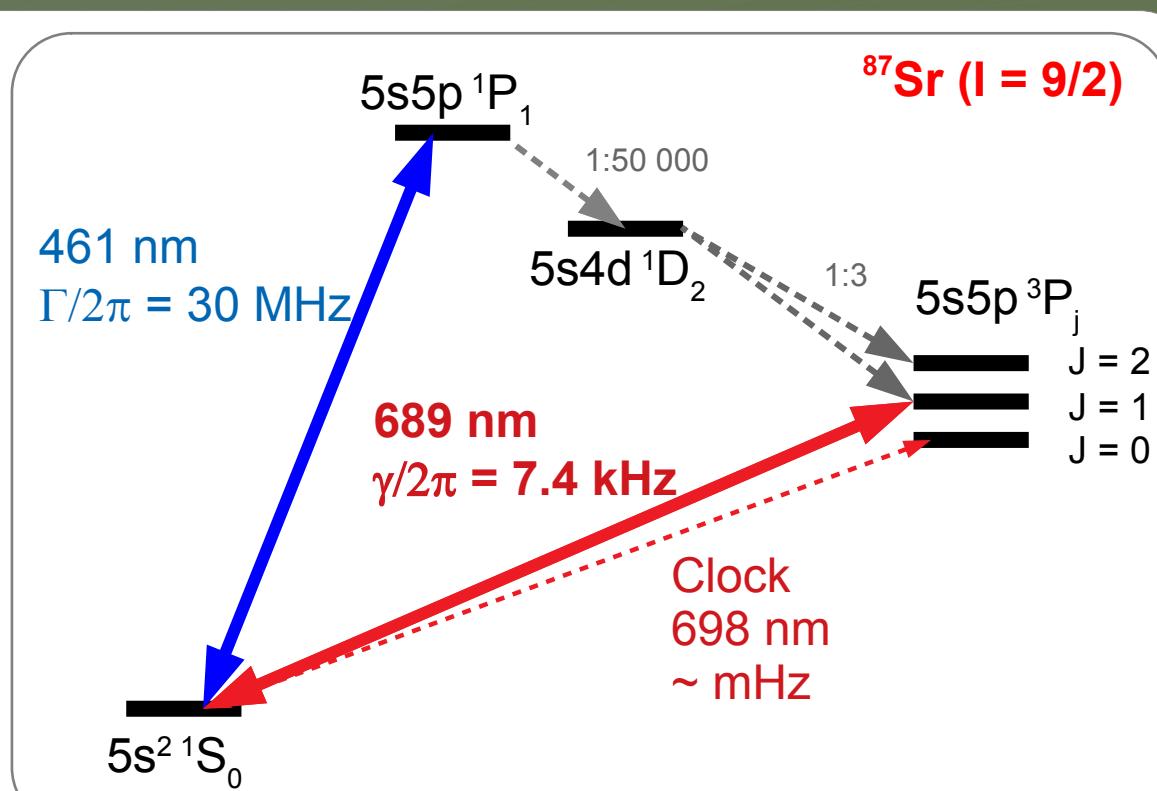
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## Narrow-lines for atomic physics

### Optical clocks

Relative instabilities  $< 10^{-16}$  at 1s  
[Ludlow 2015]



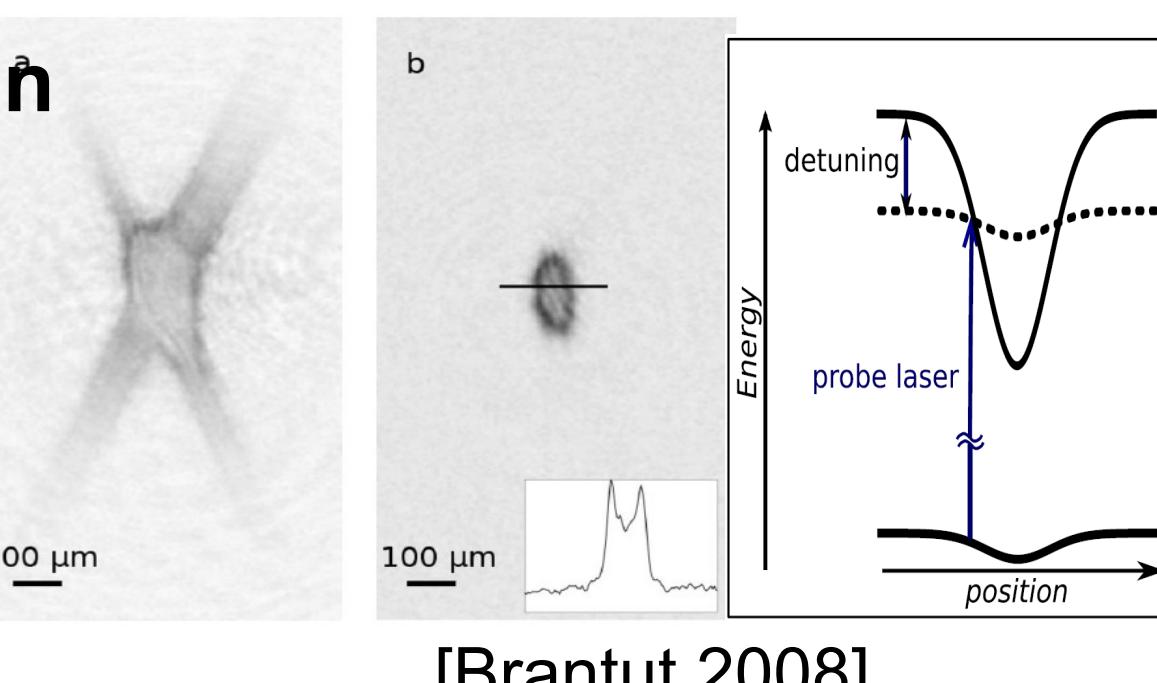
### Narrow-line cooling

- Doppler limit  $k_B T \approx \hbar \Gamma$   
1 MHz : 50  $\mu\text{K}$   $\rightarrow$  1 kHz : 50 nK
- Recoil limit :  $k_B T \sim \hbar^2 / 2m\lambda^2 \sim 500 \text{ nK}$   
[Katori 1999]

### Sensitive probes / spin manipulation

Spatial resolution in an inhomogeneous shift :  $\delta x \approx \frac{\Gamma}{\nabla \omega}$

Spin sensitivity at low field,  $g\mu_B B \gg \hbar \Gamma$

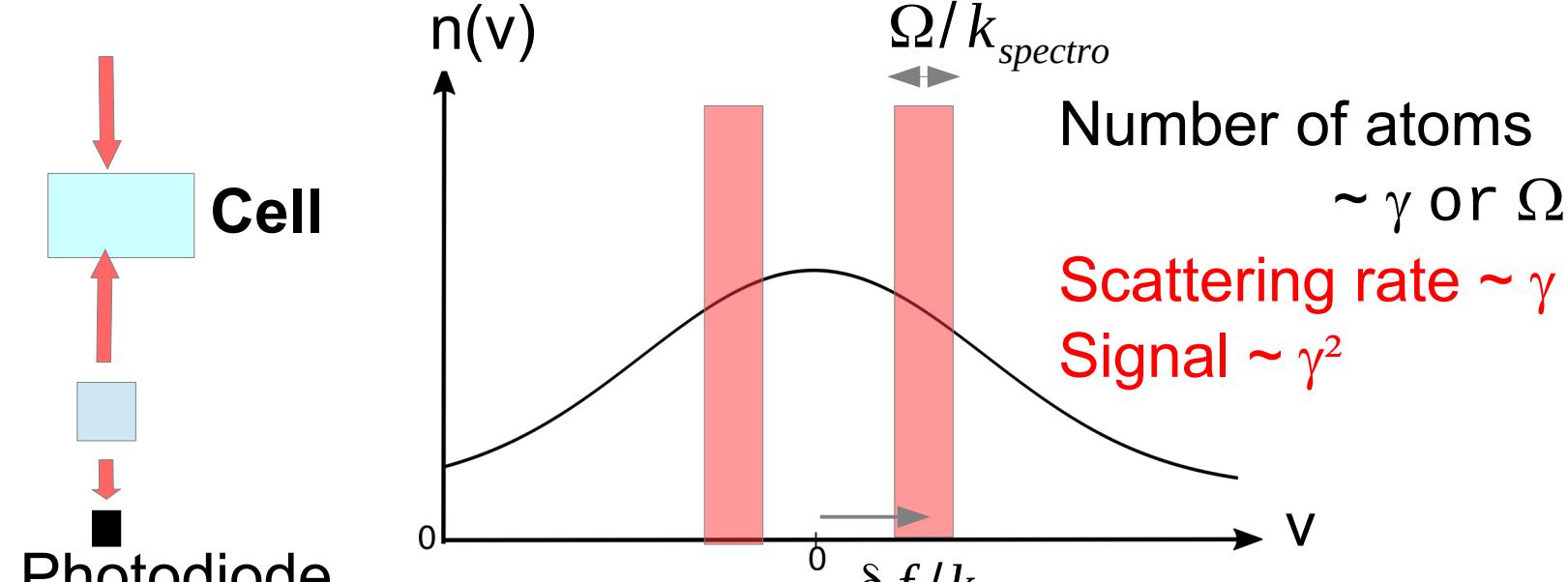


### Photo-association spectroscopy, optical control of interactions

Optical Feshbach resonances : loss rate  $K \approx \frac{2h}{m} \frac{\Gamma}{\Delta} a_{opt}$  [Yamazaki 2010]

## Frequency referencing on narrow lines

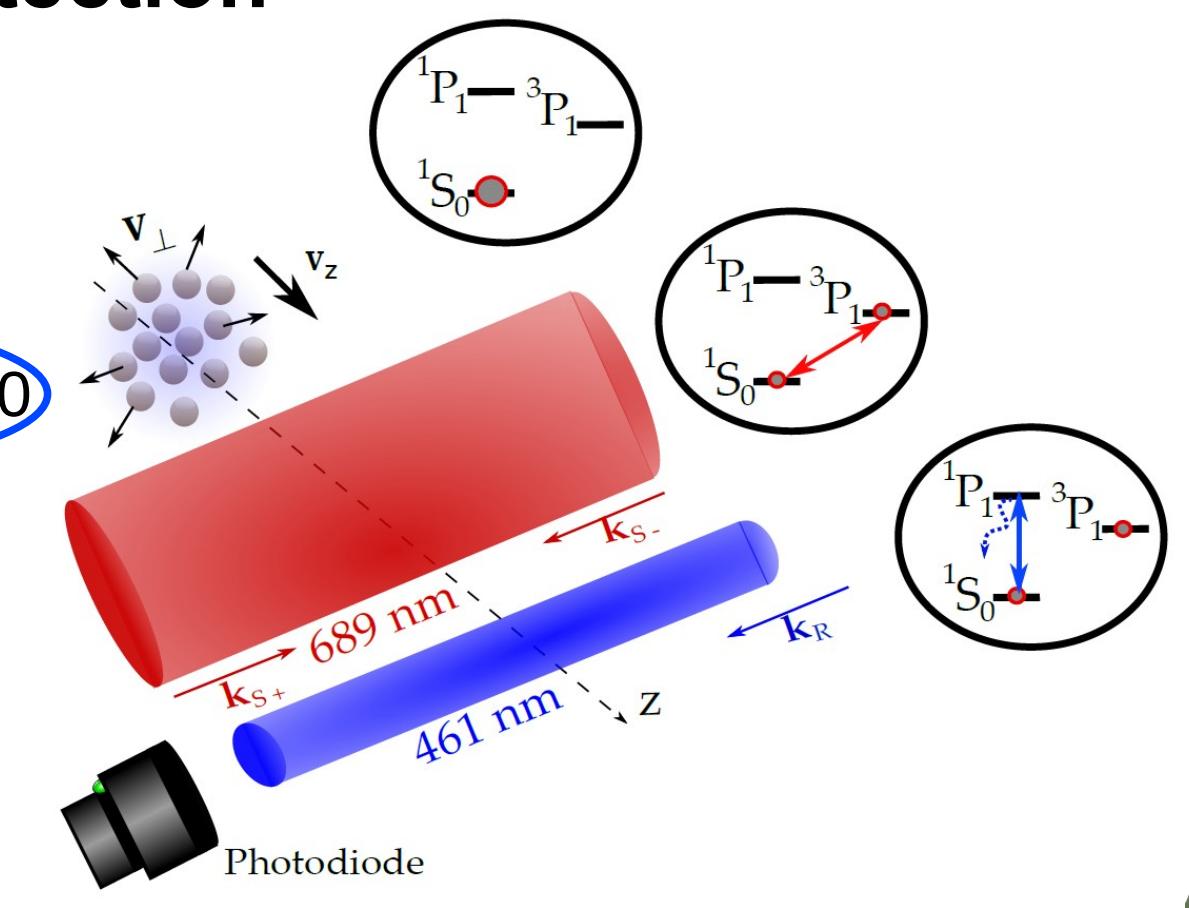
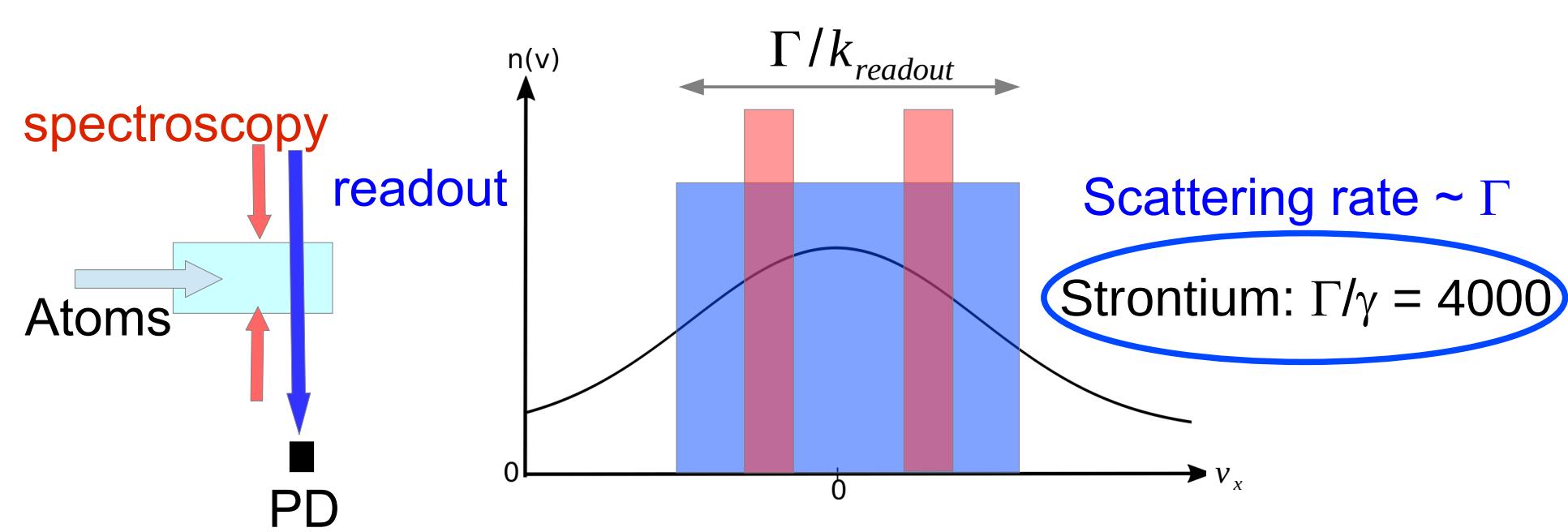
### A reduced signal in saturated absorption spectroscopy:



Saturated spectroscopy on the 7kHz-wide Sr intercombination line:

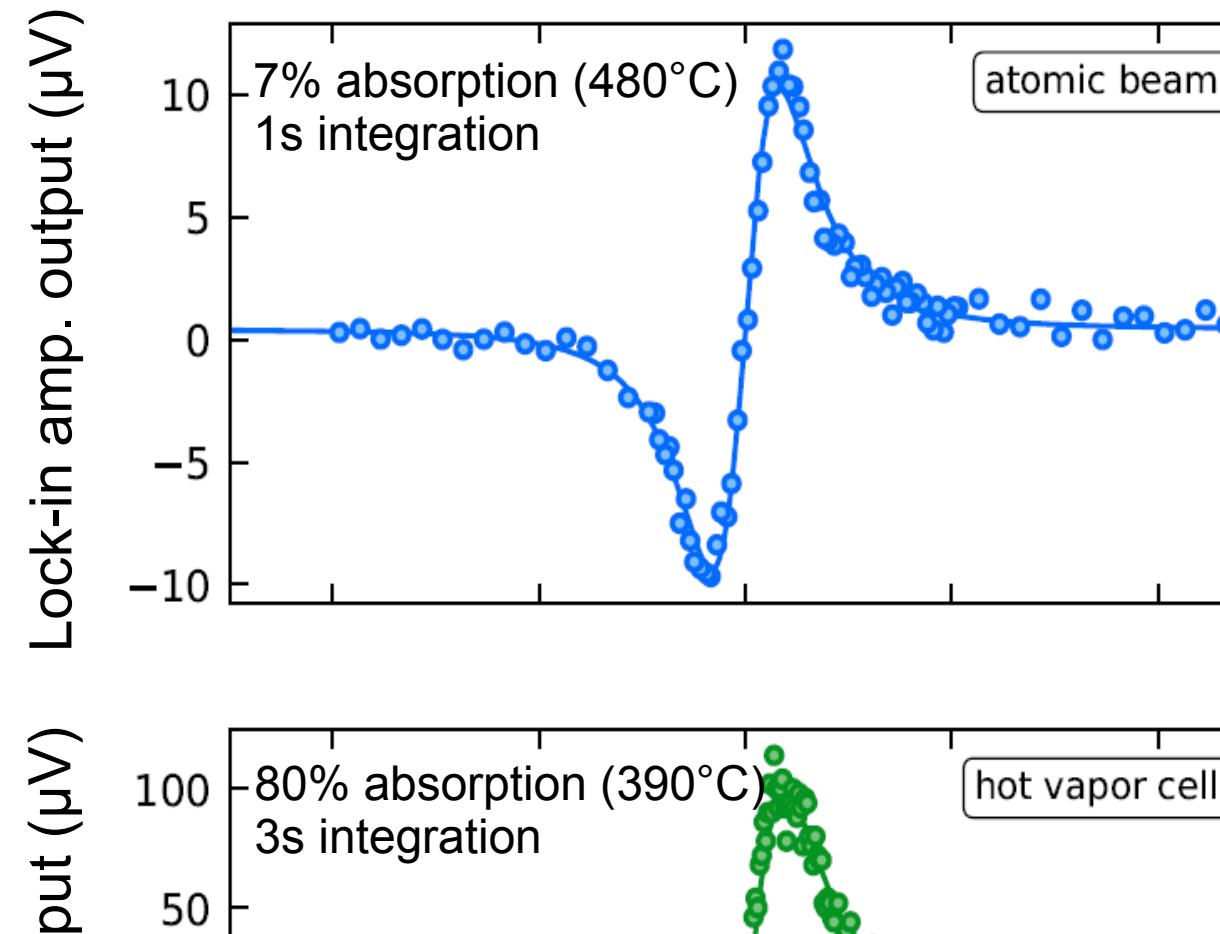
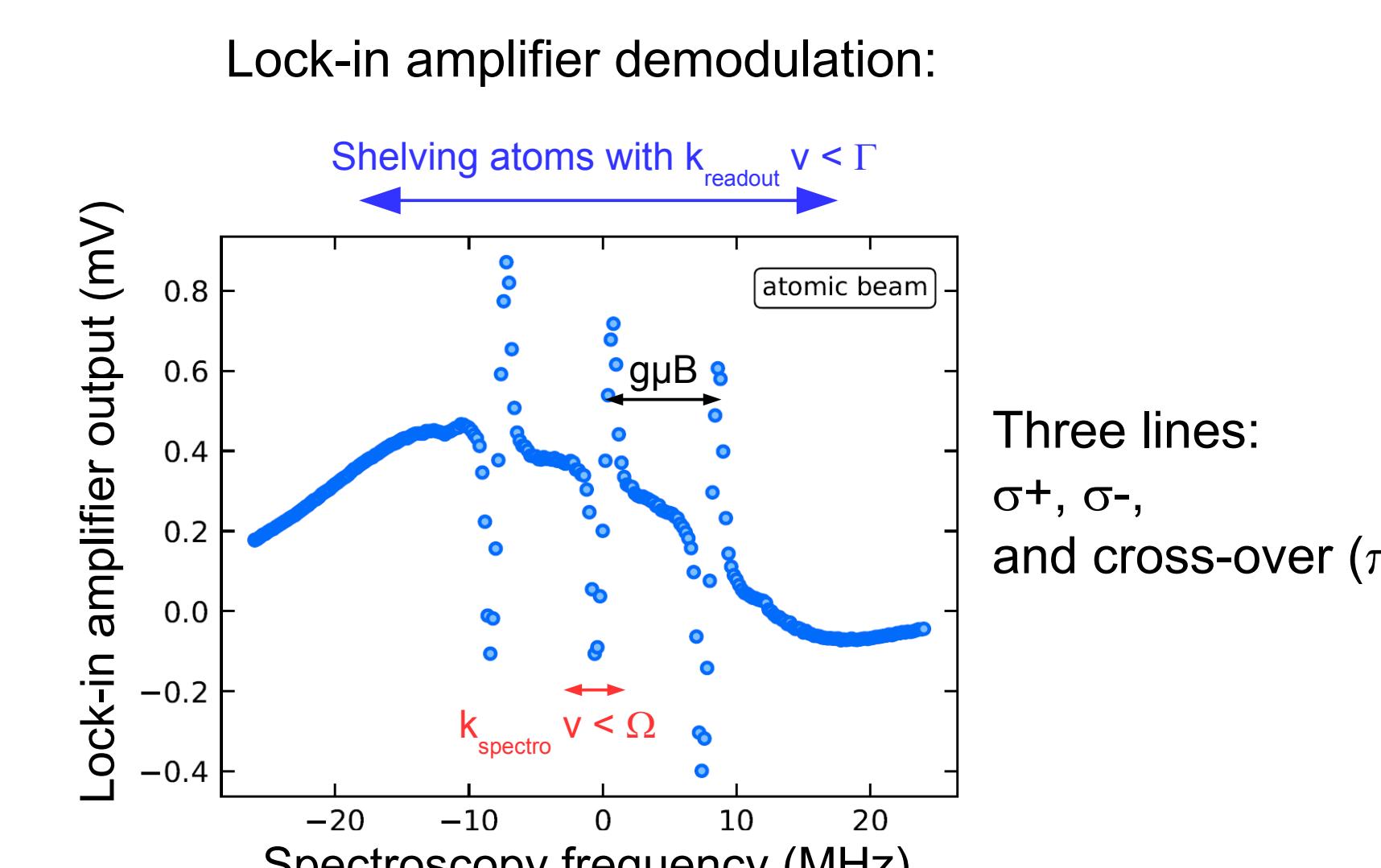
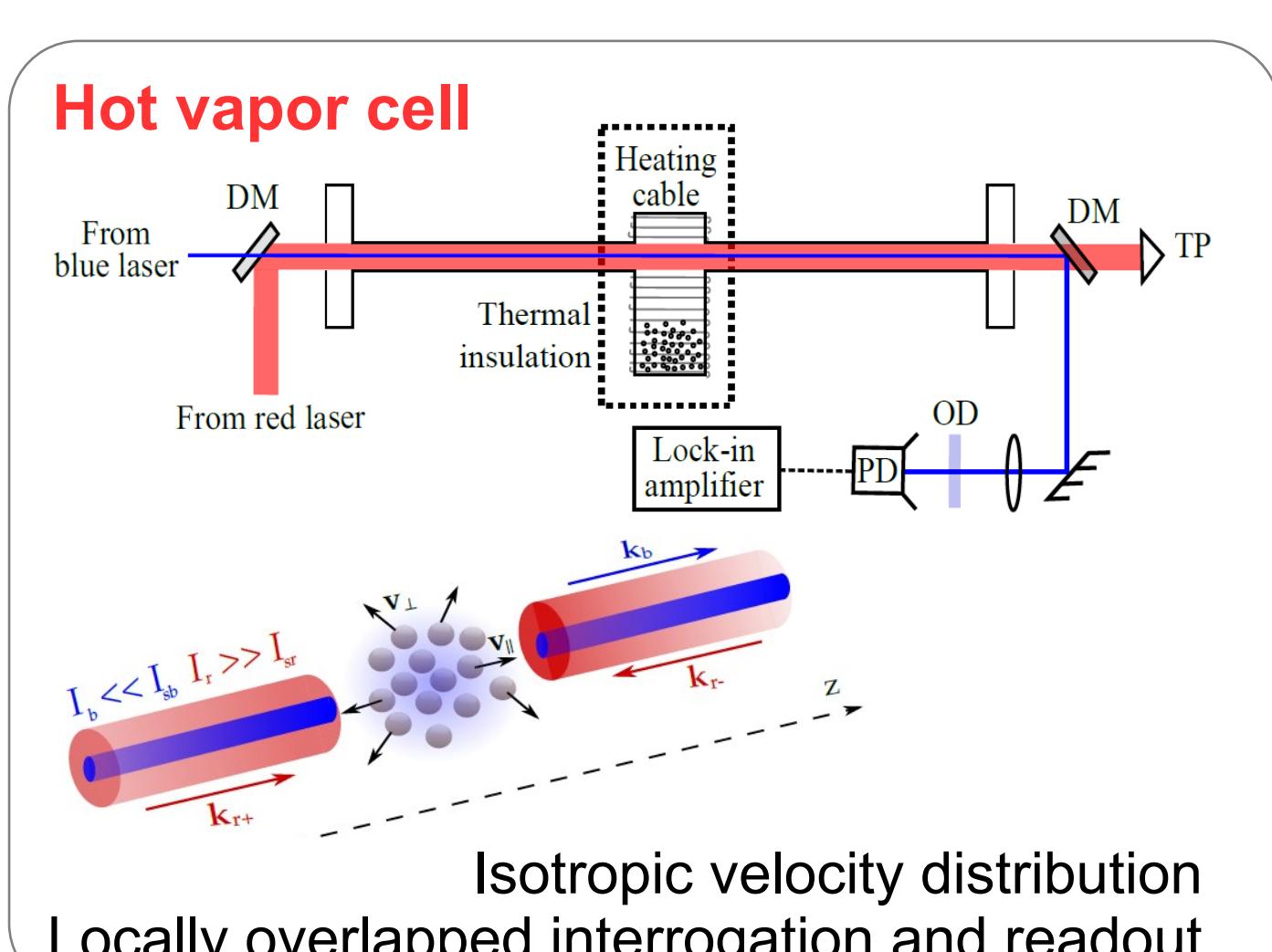
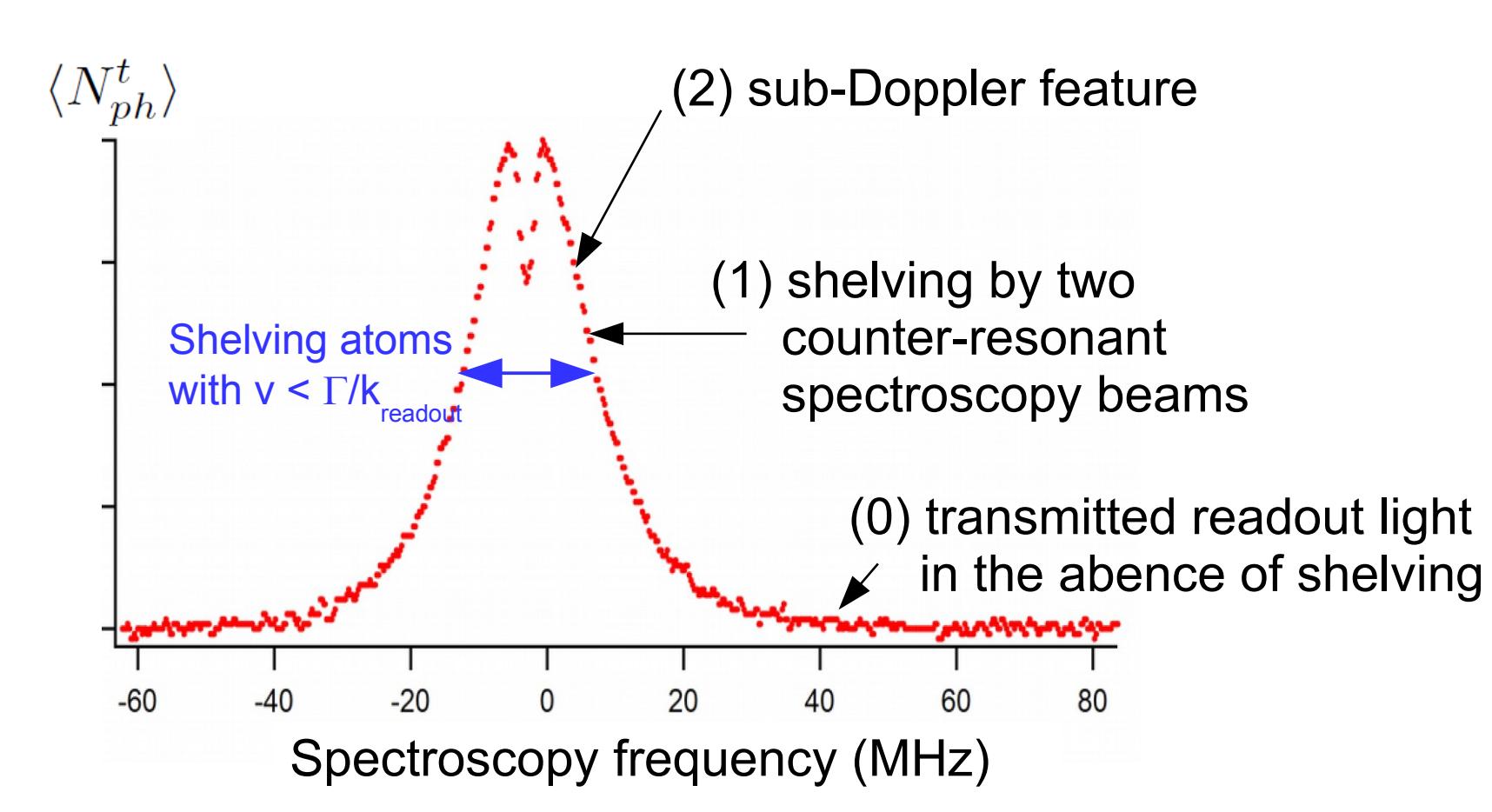
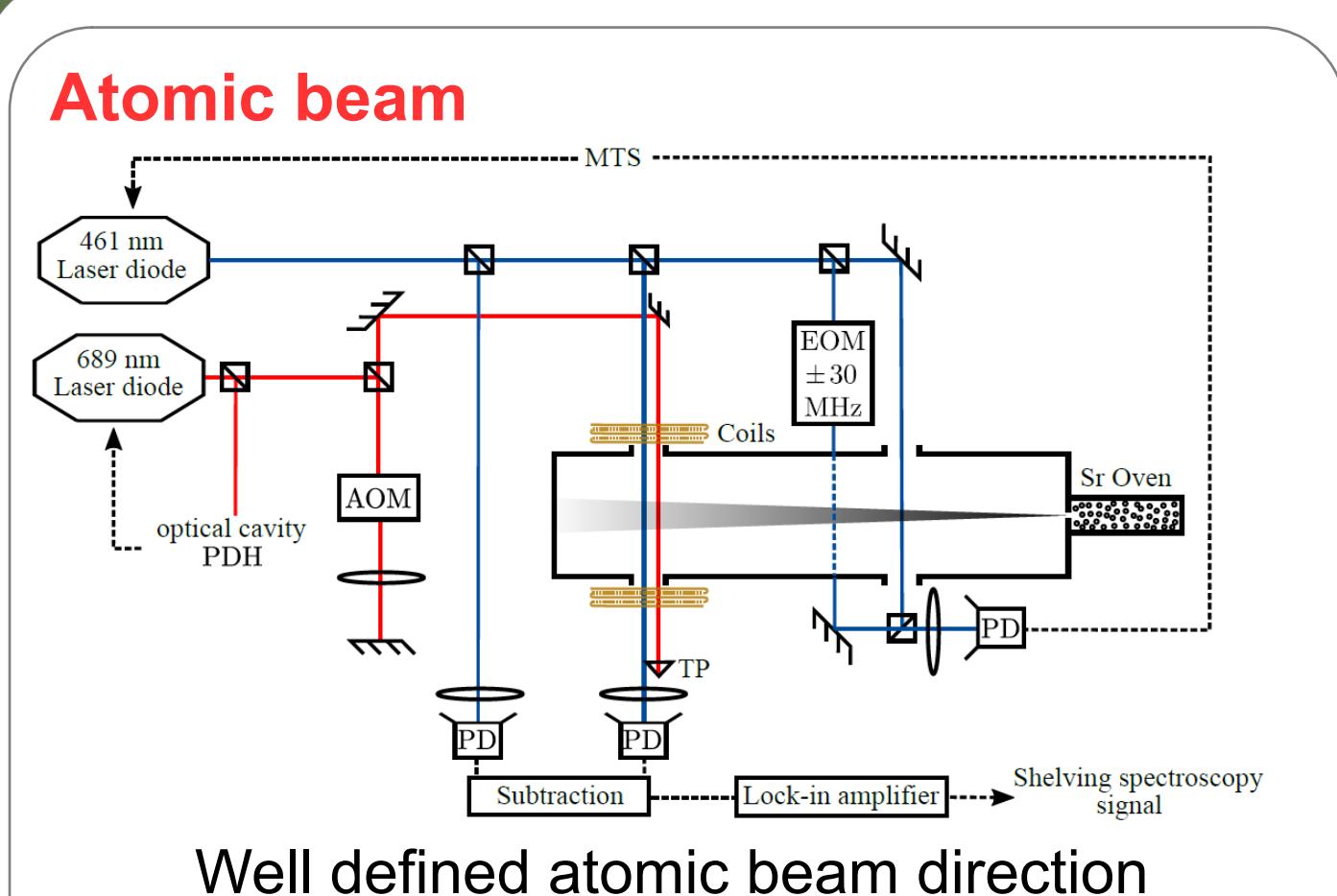
Li 2004: Hot cell  
Ferrari 2003: Atomic beam

### Enhancing the scattering rate by shelving detection



E.g. thermal Calcium beam clocks:  
Kai-Kai 2006, Mac Ferran 2009...

## Shelving detection in all settings : atomic beams and hot vapor cell



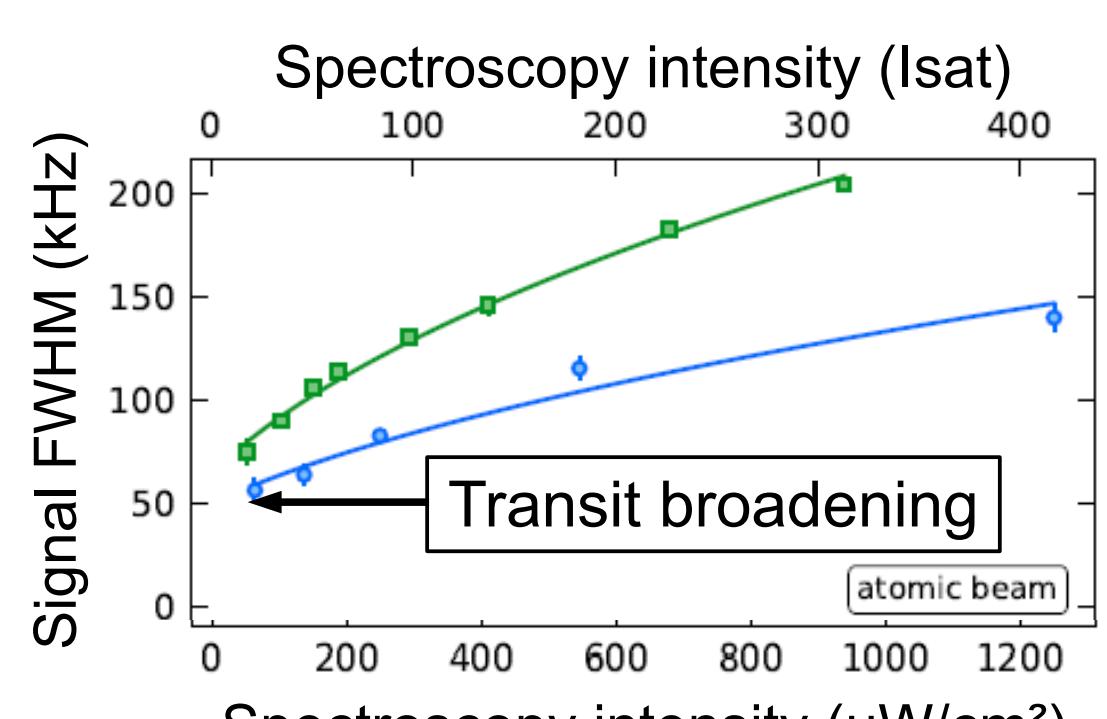
Lorentzian FWHM : 110 kHz

### Contributions:

$I = 83 \text{ Isat} \rightarrow \Omega = 50 \text{ kHz}$   
power broadening FWHM  $\sim 70 \text{ kHz}$

Modulation amplitude (p-p) 66 kHz

Transit broadening, FWHM :  $\sim 50 \text{ kHz}$



**Robust scheme**, applicable to all existing Sr cells (hot vapors and beams)

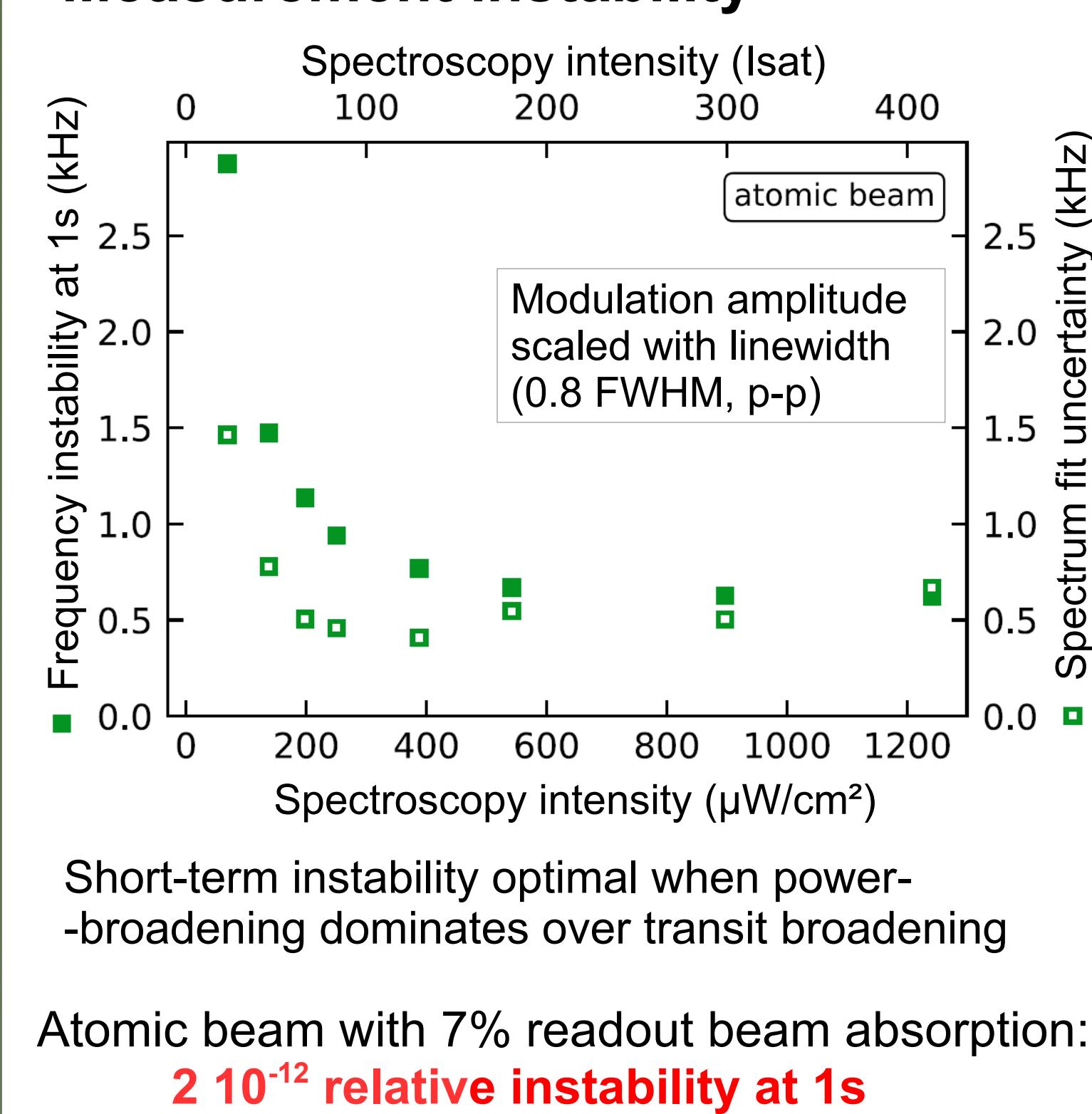
### Atomic beams:

Ramsey schemes applicable  
(and improvements, e.g. Mc Ferran 2009, Shang 2017)

Vapor cells: High absorption at low temperature (source lifetime)  
Pressure robustness (see perf.)  $\rightarrow$  no pump  
Vanishing first-order Doppler bias

## Performances

### Measurement instability



Short-term instability optimal when power-broadening dominates over transit broadening

Atomic beam with 7% readout beam absorption:  
 **$2 \times 10^{-12}$  relative instability at 1s**  
fit uncertainty 450 Hz consistent with sampling

### Measurement biases

#### 1st-order Doppler: retroreflection $\sim 50 \text{ prad}$

spectroscopy  
Atoms  $\rightarrow \vec{k}_1 \cdot \vec{v} = \vec{k}_2 \cdot \vec{v} \neq 0$   
Beam: up to 10 kHz shift, 15 kHz broadening  
Cell: symmetric broadening

#### 2nd-order Doppler: 260 Hz

Recoil doublet :  $\pm 4.8 \text{ kHz}$

AC-stark shift: 0.2 Hz

**Pressure: signal loss at  $10^{-3}$  mbar of Ar**  
**no shift or broadening detected**

Expected: 30 kHz broadening [Crane 1994]

$\rightarrow$  Hot cell: - no need for a pump  
- viewport protection by buffer gas

## Fundamental noise limitations

### Statistics of the transmitted readout light

$$\langle N_{ph}^t \rangle = \langle T \rangle \langle N_{ph}^i \rangle$$

$$\text{Var}(N_{ph}^t) = \underline{\langle T \rangle \langle N_{ph}^i \rangle} + \text{Var}(T) \langle N_{ph}^i \rangle^2$$

Photon shot noise      Effect of atom shot noise on the transmission

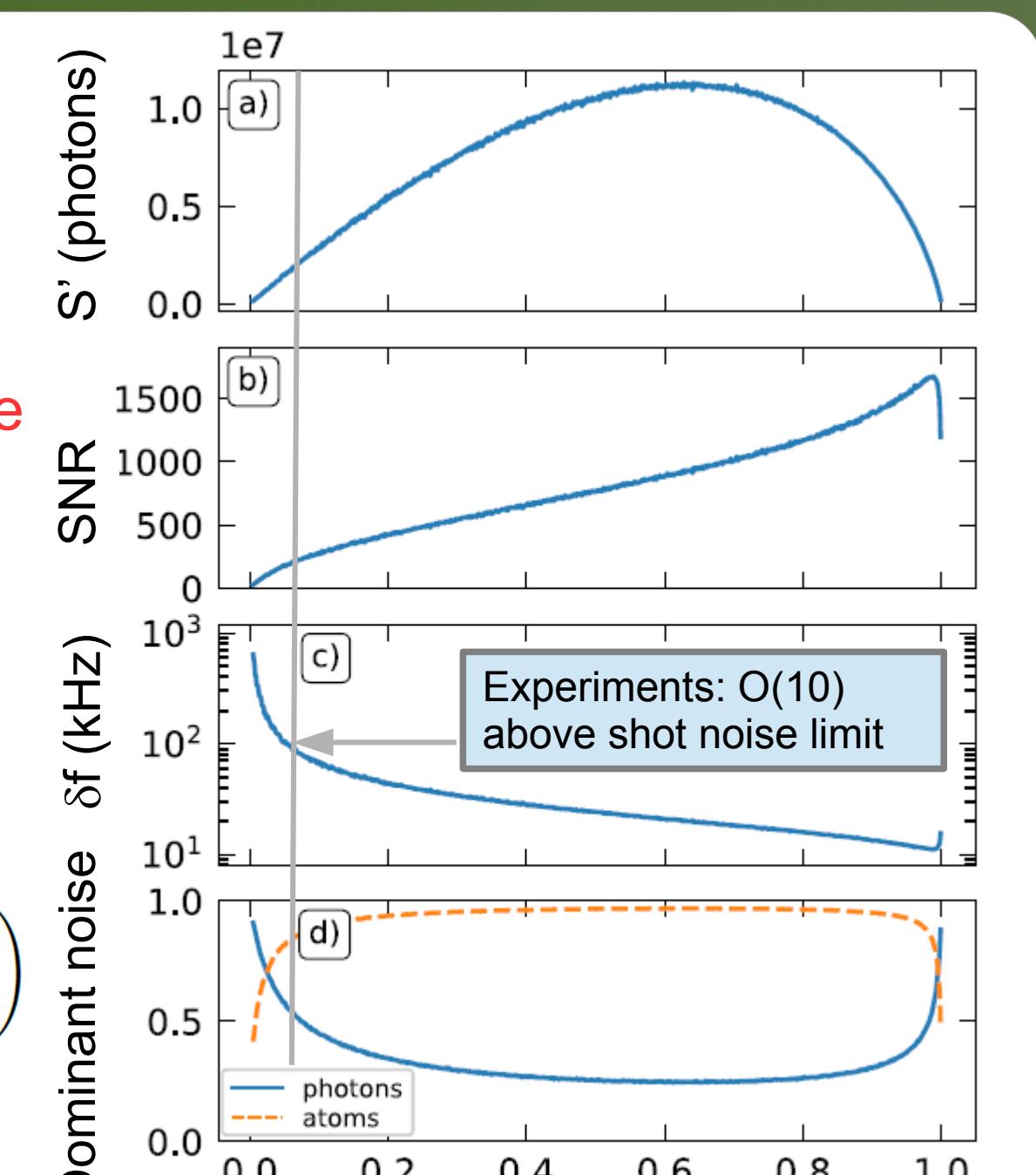
Advantage of shelving detection:  
relative photon shot noise can be low

### Spectroscopy instability

$$S' = G \left( P \tau \frac{\lambda_R}{hc} (1 - A^{(2)}) \right) - G \left( P \tau \frac{\lambda_R}{hc} (1 - A^{(1)}) \right) = G \left( N_{ph}^{t,(2)} - N_{ph}^{t,(1)} \right).$$

$$\text{SNR} = \sqrt{\frac{t_{\text{integ}}}{2 t_{\text{sample}}}} \cdot \sqrt{\frac{(\langle N_{ph}^{t,(1)} \rangle - \langle N_{ph}^{t,(2)} \rangle)^2}{\text{Var}(N_{ph}^{t,(1)}) + \text{Var}(N_{ph}^{t,(2)})}}$$

$$\delta f = \frac{\gamma(I) 3\sqrt{3}}{2\pi} \frac{1}{32} \frac{1}{\text{SNR}}$$



Strong improvement achievable:  
**at high densities,  $3 \times 10^{-14}$  at 1s**

**Very similar to Ca-beam clocks,**  
e.g. McFerran 2009:  $7 \times 10^{-14}$  at 1s

## Outlooks

### Shelving spectroscopy

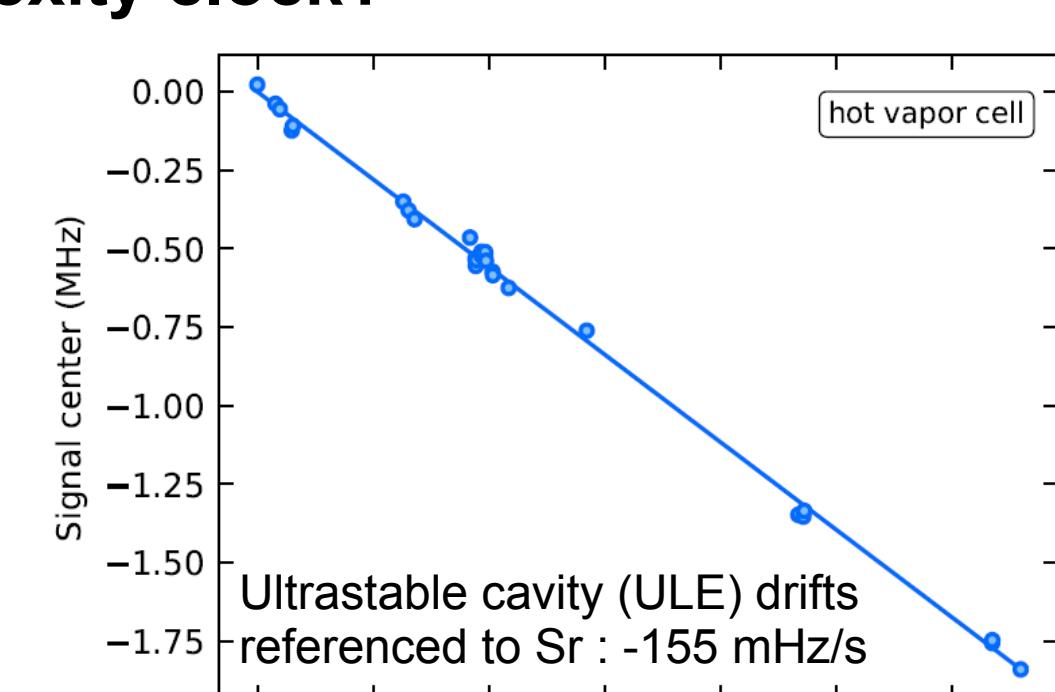
Robustness and ease of implementation:

**applicable to all kinds of cell**

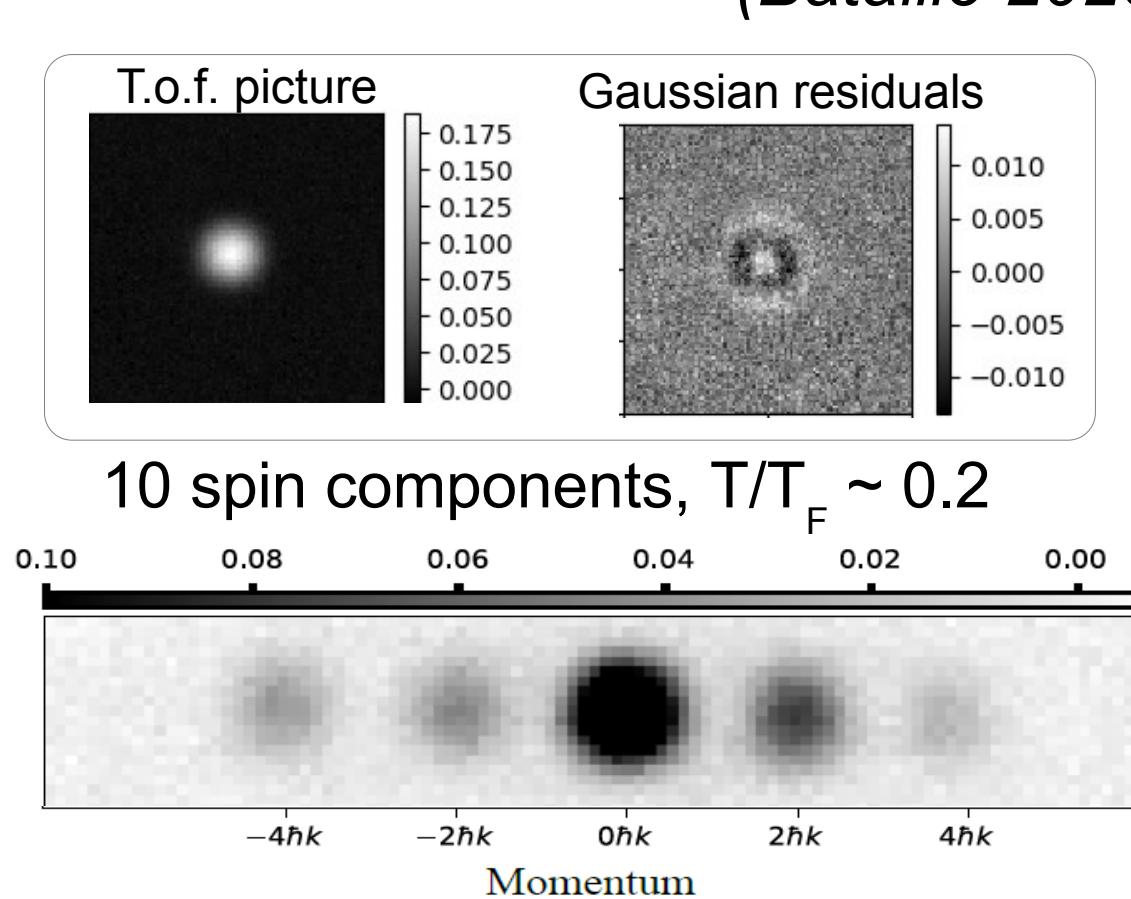
Expected performance limitations  $\sim 10^{-14}$ :

**a future as low-complexity clock?**

Experiments outlook:  
characterization of the  
**long-term stability**  
(requires a second  
absolute reference)



**Other progresses:** - SU(10)-symmetric Fermi sea of  $^{87}\text{Sr}$   
- Adiabatic spin-dependent momentum transfer (Bataille 2020)



## References

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